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Abstract

Researchers have long proposed using economic approaches to resource allocation in computer systems. However, few of these proposals became operational, let alone commercial. Questions persist about the economic approach regarding its assumptions, value, applicability, and relevance to system design. The goal of this paper is to answer these questions. We find that market-based resource allocation *is* useful, and more importantly, that mechanism design and system design should be integrated to produce systems that are both economically and computationally efficient.

1 Introduction

A key advantage of the Internet, peer-to-peer file sharing networks, and systems like PlanetLab [1] is the sharing of computational resources. This provides a variety of benefits, including higher utilization, increased throughput, lower delay (due to dispersion of resources in the network), and higher reliability. However, resource allocation remains an issue. The problem is how to allocate a shared resource fairly, with economic efficiency (where efficiency is the ratio of the total actual benefit to all users to the optimal benefit), and at low cost.

Scheduling algorithms like Proportional Share are a partial solution. The problem with PS is determining how to set the weights. Assuming that the values of tasks varies over time, no single set of weights will suffice. Setting of weights cannot be left to users because they have a strong incentive to always ask for the highest possible weight. Having the system administrator set weights is error-prone and time-consuming.

Economics and game theory offer an alternative. The area of *mechanism design* is concerned with algorithms where individuals optimizing their own utility results in high overall utility. A market (or auction) is an example. In the resource allocation context, as users optimize the benefit that they receive from their applications, the mechanism optimizes the overall efficiency of the resource allocation, without the intervention of an administrator.

This is not a novel idea. Researchers [6] [9] proposed this approach as early as 1988, and there were likely earlier ones. Since then, several researchers [16] [11] [13] [2] [10] have pursued it. Unfortunately, there have been few implementations [16] [2] [4]. Given 17 years of research, it is surprising that there is not even one commercially or freely available system for market-based resource allocation. Given the impact of poor resource allocation on systems like PlanetLab, this appealing approach and a large body of enthusiastic publications, why have so few systems been built? We believe the lack of operational systems is because questions persist in the minds of system designers about the value of the economic approach, its applicability, and its relevance to system design.

In this paper, we examine some of these questions using a combination of qualitative arguments and simulation. We do not claim to have conclusive answer. Instead, we hope to provide sufficient affirmative evidence that more real systems should be built, deployed, and evaluated.

2 An Example

In this section, we examine Proportional Share (PS) scheduling as an example of the problem that marketbased resource allocation seeks to solve. PS gives user iwith weight $w_i a w_i / \sum w$ share of the resources. Using PS hierarchically, the user can assign these resources to his tasks. For example, if Alice has weight 2 and Bob has a weight of 1, then Alice has two-thirds of the total resources for her tasks and Bob has one third. Suppose that this is necessary because Alice must process twice as many queries as Bob. This works well if Alice is always doing something more important than Bob, but sometimes Bob will have an important task (e.g., serving a client query) while Alice has a much less important task (e.g., non-time-critical background jobs like garbage collection). In this case, Alice's task will still get most of the resources. This is an economically inefficient situation because although Alice receives some small benefit, Bob receives much less than he could, and the total benefit is much less than if Bob received most of the current resources. This is a common situation because for most users and their applications. the arrival process of important work is highly bursty (e.g., a web/email/file server).

One solution is to rely on Alice to yield resources (e.g., using **nice** or other means to set lower weights on tasks) when doing less important tasks. Unfortunately, Alice has an incentive to deny Bob the resources

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and use them herself. This is an example "Tragedy of the Commons" [7] where optimizing for individual utility results in low overall utility. On the other hand, optimizing for overall utility depends on knowing the relative values of every task being run. Unfortunately, users cannot be relied on to accurately report these values without an honesty incentive. Some users may behave *obediently* by yielding resources or honestly reporting task values, but those that do not (*strategic* users) lower the efficiency of the system, and, worse, provide an incentive for obedient users to become strategic.

Another solution is to have a system administrator monitor the system and dynamically change the weights of the users to maintain high efficiency. However, this is expensive, time-consuming, and errorprone, and it is does not scale to large numbers of users and resources.

Market-based resource allocation addresses this problem. For example, Alice and Bob are issued a currency with income rates in the ratio 2 to 1. They use these credits to bid for resources in a market where user i with bid b_i receives a $w_i / \sum w$ share of the resources. When a user has used her share, then her bid is deducted from her balance of credits. Since Alice is aware that garbage collection is a less critical task than serving client queries, she will spend fewer credits when doing the former and more doing the latter. The mechanism provides an incentive for users to truthfully reveal how much they value resources. This allows Bob to get more resources than Alice when he is processing queries and she is doing garbage collection. Over the long-term, Alice can still process twice as many queries as Bob (assuming similar workloads).

3 Resource Allocation Markets

In this section, we examine some questions about market-based resource allocation.

3.1 What benefits do markets provide over long-term PS?

In long-term Proportional Share, user *i*'s share of the resources is $w_i / \sum w$ over a longer time period (e.g., a week or year) than the 10 milliseconds of a typical CPU scheduler. This provides some of the flexibility of a market-based system.

However, long-term PS is not sufficient to reach economic efficiency. It does not encourage users to shift usage from high demand periods to low demand periods. It also does not encourage users to shift usage from high demand resources to low demand resources. For example, a system could have high demand for CPU cycles, but low demand for physical memory. In a typical application of PS, the CPU and memory would be allocated separately and applications would have no incentive to use more memory and fewer CPU cycles [14].

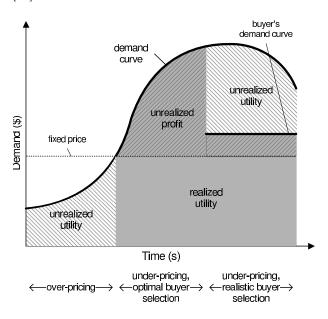


Figure 1: **Fixed and Variable Pricing.** This figure shows a variable demand curve over time and how its efficiency compares to a fixed pricing curve.

A related solution is to use fixed pricing. For example, each CPU cycle costs \$10 and each memory page costs \$1. A user in this example has a strong incentive to use more memory to save CPU cycles, so this begins to address the multi-resource problem. Pricing also provides a way for applications to express quality-of-service needs. For example, an application may not need many cycles, but instead needs them quickly after an interrupt has occurred [5]. Time slices could be priced differently based on how quickly they are scheduled.

The problem is how these prices should be set. Figure 1 shows that no fixed price is as efficient as a variable price, assuming variable demand. In the left regime, the demand is below the fixed price, so the buyer is unwilling to buy the resource and the utility that the buyer would have gained by using the resource is unrealized (indicated by the striped area under the demand curve). In the middle regime, someone is willing the pay the fixed price, so that buyer is able to use the resource and gains some utility (indicated by the gray area under the demand curve). Assuming that the seller chooses the optimally efficient buyer (i.e., the one willing to pay the most), then the difference between the demand curve and the fixed price is unrealized profit for the seller (indicated by the striped gray area). Unrealized profit contributes to overall inefficiency in some cases (see § 3.3). However, without a covert channel, a fixed price seller cannot distinguish among the demand curves of potential buyers, so the actual buyer's demand curve will probably be lower than the optimal buyer's and the area between them is more unrealized utility. In general, the more variable the demand, the worse the efficiency loss of fixed prices.

One definition of a market is a way to set prices so that they follow the demand. As a result, most, if not all of the utility under the demand curve in Figure 1 would be realized.

3.2 Are markets fair?

Markets allow users to save currency. Could this allow a user to save enough currency to starve out other users? Are markets unfair in some other way?

Whether markets are fair depends on the market and the definition of fair. One definition is that all users receive resources in proportion to an exogenously determined weighting system. For example, if Alice has a weight of 2 and Bob has a weight of 1, Alice should get twice the resources of Bob over an arbitrarily long time interval. Assuming that Alice and Bob have demand curves that equally correlated with the overall demand, the market described in § 2 is fair by this definition.

One variation of this definition is to restrict the timescale used to measure the resource usage. For example, within an hour interval, if Alice and Bob want resources, she should always get twice the resources that he gets, even though he saved up his credits and she spent hers. This is useful to prevent starvation by those who mis-manage their resources. Another possibility is that Bob saves up credits over a long period of time and then spends them all at once, thus starving out Alice. In both cases, the system can monitor Alice and Bob's credits and redistribute credits from the wealthy to the poor. This reduces the degree of unfairness, but also reduces efficiency because Alice and Bob have a reduced incentive manage resource usage carefully.

The conclusion is that markets are not inherently unfair. System designers can tune a market-based system to make the tradeoff between efficiency and fairness that is appropriate for their users.

3.3 Are markets useful when real money is not involved?

Economic mechanisms provide an intuitive mapping between resource allocation and a business model for selling resources. However, in some cases, the resources are just being shared and not sold (e.g., employees sharing machines in their company's data center).

Markets are still useful in these situation. The simplest configuration is an open-loop economy, where the resource owner issues credits to users who can then spend them on resources. The main efficiency gain results from users having an incentive to truthfully reveal the value of their tasks (as shown in § 4).

Another alternative is a closed loop economy where users both consume and provide resources. PlanetLab could be run this way. A closed loop economy provides more incentives for efficiency than an open loop one: as prices rise, so does providers' profit, which increases the incentive to provide resources. This raises competition and eventually causes prices to fall. At no point in this cycle is real money necessarily involved.

3.4 Are markets predictable?

Markets may allocate resources efficiently on average, but prices for resources fluctuate, so how can users predict the cost of the resources that they need?

In this context, we define predictability (i.e., performance isolation or quality-of-service) as the ability to provide a fixed amount of resources over a period of time with high probability, regardless of the demand put on the system. An example of an application needing predictability is a web server that needs to serve nrequests per second with 99% of requests served within d seconds.

The market from § 2 can provide this capability by adding the ability to reserve fixed shares, where a share is a fixed percentage of a resource (e.g., .1% of a 1 GHz CPU = 1 MHz). These shares have a fixed duration and are sold using an auction. The operator of the example web server calculates the resources necessary to meet his needs and bids for those resources. The cost of this approach is that resource may be underutilized because some resources may be reserved, but go unused.

Although similar to techniques used in non-market systems [12] [14] [5], the market allows the predictability mechanism to be used more efficiently. The problem with these systems is the difficulty in deciding how much of the resource should be devoted to best-effort service and how much to reserved service. The optimal split will likely vary significantly over time. Users would prefer reserved service if the cost to them is equal, but reserved resource are less efficient than besteffort because of the potential for under-utilization. The benefit of the market is in forcing users to consider whether they really require reserved resources and in helping the system determine reserved/best-effort split. High bids for reserved service will cause users who can

Parameter	Value
Users	10
Running Time	1000s
Task Interarrival	Gaussian, μ : [1s, 120s], σ : $\mu/2$
Task Size	Gaussian, μ : 10, σ : 5
Task Deadline	Gaussian, μ : 75, σ : 37.5
Task Value	Uniform, range: $(0, 1]$

Table 1: Simulation parameters

tolerate best-effort to do so and indicate to the system to reserve more resources. Low bids will do the opposite.

4 Simulation Results

In this section, we present preliminary simulation results quantifying the efficiency gains of a market. The basic idea is to simulate a single CPU server running the CPU-intensive tasks of several users. We examine different resource allocation algorithms and different user behaviors.

The simulation parameters are summarized in Table 4. A user may have more than one pending task, but users only run one task at a time. If a task completes by the deadline, then the user receives *value* * *size* utility, otherwise There is one server providing resources for tasks. A task finishes when it accumulates resources equal to its size. A user can run one task, switch to a new task, and then switch back to the first task without cost.

The server uses one of two resource allocation schemes: Proportional Share or Market Proportional Share. With Proportional Share, the server allocates its resources to tasks according to the weight assigned by the task's owner. With Market Proportional Share, users have an income of \$1 credit per second. If Alice spends 1 credit and Bob spends 2, then Alice's task gets .66 resources, while Bob's task gets .33. The income can be saved.

We simulate three different user behaviors: obedient, strategic without a market, and strategic with a market. Obedient users assign a weight to their tasks equal to the task's value. Non-market strategic users assign the maximum possible weight to all of their tasks. Market strategic users budget their credits according to the task. The idea is to spend more credits on more valuable tasks and to apportion the credits over the lifetime of the task. Market strategic users assign the following credits per second to run their most valuable task: (balance * value)/(deadline - now). balance is the user's current credit balance, value is the value of the user's most current valuable task, deadline is the deadline of that task, and *now* is the current time.

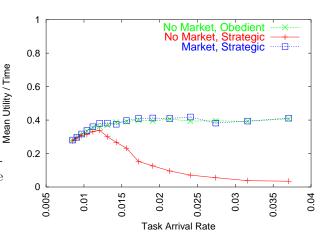


Figure 2: The utility of different user behaviors and mechanism as a function of system load.

Figure 2 shows the simulation results. The y-axis is the mean utility per host per time unit. The x-axis shows the mean task arrival rate in the system and is a measure of overall system load. Each point in the graph is a run of the simulator.

As the load increases to the right, the obedient users without a market are able to maintain a high level of utility. However, users have no incentive to be unilaterally obedient. Instead, their incentive is to strategically give a high weight to all their tasks. The plot of the non-market strategic users shows that they are able to maintain a high level of utility when the system is lightly loaded (from 0.0 to 0.0125), but as the load saturates the system, utility drops to zero. At this point the system wastes resources running tasks that never meet their deadlines and therefore provide no utility. In a system without a mechanism or significant social pressure, some users inevitably become strategic. To counter this, we use the market mechanism. The strategic users are forced to truthfully reveal the value of their tasks and the system can maintain the same high level of utility as when all users were obedient.

5 Integrated Mechanism and System Design

Mechanism design is traditionally part of economics while system design is part of computer science. Why should they be done in concert? How much benefit would be provided by adding an existing mechanism, such as bartering or EBay, to a separately designed system?

A long-standing principle [8] in system design is to separate policy and the computational mechanism used to implement the policy (not the economic mechanism in the mechanism design sense). However, as Clark, et al. [3] point out, policy and computational mechanism cannot truly be separated because the mechanism defines what policies are possible.

This would not be a problem if computational mechanism designers provided interfaces for efficient and scalable policies, but this has not been the case. For example, the market from § 2 requires statistics on resource usage (e.g., CPU cycles, memory pages, disk blocks) and dynamic control over allocation. However, many systems do not export detailed information on usage or allow dynamic control of allocations [15]. Another example is that several computational mechanisms assume a bartering policy. However, bartering economies have very little fluidity. It is difficult to find a mutually satisfying partner for each transaction and the complexity of determining the exchange rates of nresources is $O(n^2)$.

Even using an efficient economic mechanism from other contexts can result in poor efficiency in a computational environment. Unlike many other resources, the latency to access a computational resource is critical because changes in demand are unpredictable. For example, one possible economic mechanism for computational resources is to auction them on EBay. Auctions on EBay are tuned for human bidding so they typically take hours to close. The problem is that a web server's demand may be spiking right now. By the time the auction closes, the high load will have dissipated. The web server's operator could try to anticipate load and purchase capacity in advance, but this results in unused capacity.

In general, a pure mechanism designer is likely to design an economic mechanism with high economic efficiency, but with little concern for traditional systems metrics of computational efficiency, reliability, security, complexity, and ease-of-use. Pure systems designers have generally done the inverse. This is a direct consequence of a strict interpretation of the policy/mechanism separation principle. Instead, we advocate that systems designers embrace mechanism design as a first-order concern to eventually produce systems than can be both economically and computationally efficient.

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